

# DYNAMIC MODELS FOR A HEAT-LED ORGANIC RANKINE CYCLE

- turbine and alternator models

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## Motivation for the work

- 150 biomass based power plants all over Europe, 140 are heat-led
- many facilities are suffering from economic difficulties (fuel prices  $\uparrow$  , feed-in tariffs  $\downarrow$  , maintenance  $\uparrow$ )
- heat-led systems have limited degrees of freedom
- previous analyses have shown problems of control system regarding varying loads
- therefore, necessity for control optimisation

# System overview I

Table : Design data of case study plant

-	Value	Unit
Thermal input	6356	kW
Temperature of source	300/240	°C
Thermal output	5300	kW
Temperature of sink	80/60	°C
Electric output	950	kVA
Mass flow	20	kg/s
Gross design efficiency	16.38	%

# System overview II

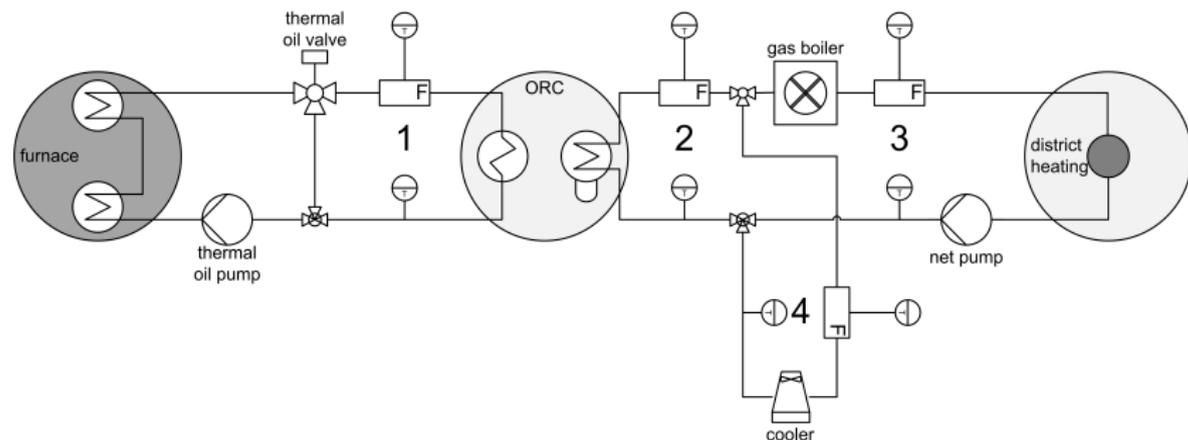


Figure : furnace, transfer system, ORC, cooling unit, district heating

- Fluids: thermal oil (T66), Octamethyltrisiloxane (MDM), water
- Heating curve is based on amb. temperature /ORC control is heat-led

# Cycle layout

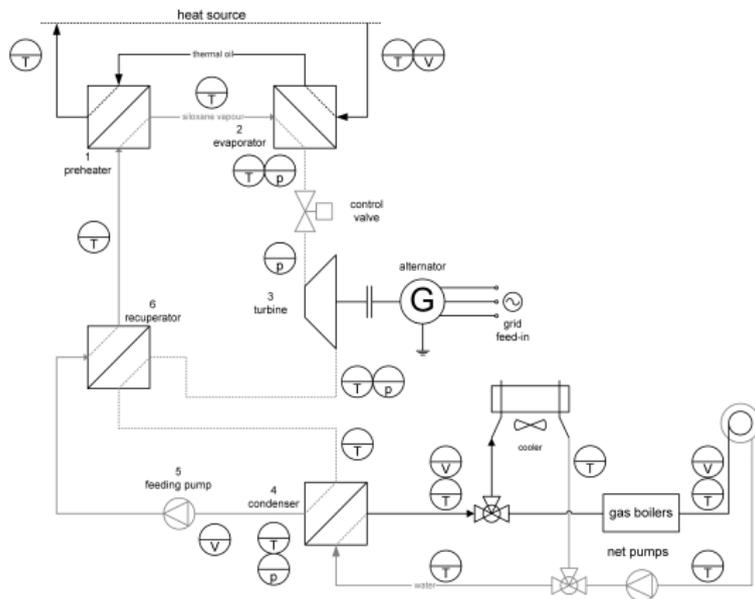


Figure : cycle including all relevant sensors

# Simulation scope I

## Overall scope

- find compensation strategies for the controller
- find a suitable winter, summer and intermediate operation strategy

## Partial scope

- dynamic generator model: improve validation, simulate start-stop procedures, alternator oscillation

→ a very accurate and robust turbine, alternator and drive shaft model with a wide load range is required.

# Simulation method I

## Method

- physical turbine model with empirical correlation for stage efficiency
- empirical alternator model based on design data of manufacturer
- physical drive train model
- validation through: measured electric output,  $\sum \dot{m}$ , frequency
- validation data for three different load ranges: high, medium, low

## Tools

- steady state calculations, correlation fitting → MATLAB
- dynamic simulation → Dymola 2013 / modelica
- *ExternalMedia* Lib, *FluidPropMedium* Package, REFPROP [3]
- *ThermoPower* Lib

# Turbine I

## Turbine

- type: impulse, axial, single stage, super-sonic
- nozzle: 24 x De Laval,  $\alpha = 19^\circ$ ,  $\eta_{noz} = 92\%$
- turbine speed 3000 RPM  $\rightarrow \bar{u} \sim 160$  m/s
- isentropic outflow velocity: 300 m/s
- lubrication system: separate
- frequency control: alternator/grid
- flow control: full admission, control (by-pass) valve for start-up
- mean rotor diameter 1 m

# Turbine II



Figure : turbine, diffuser and aux. compounds

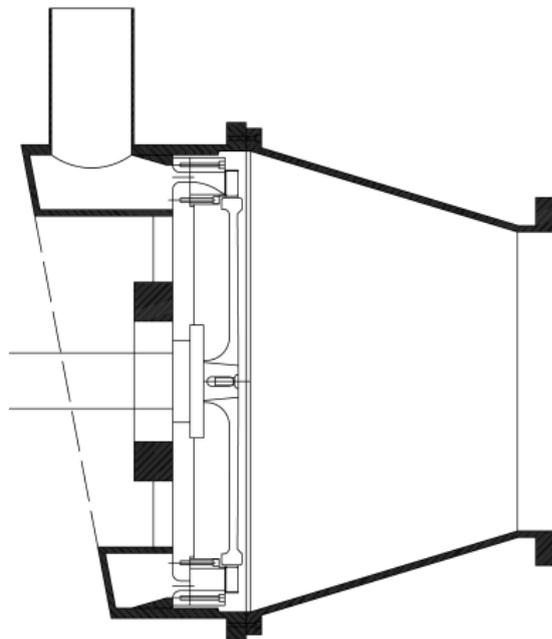


Figure : cross section of turbine and diffuser

# Turbine III

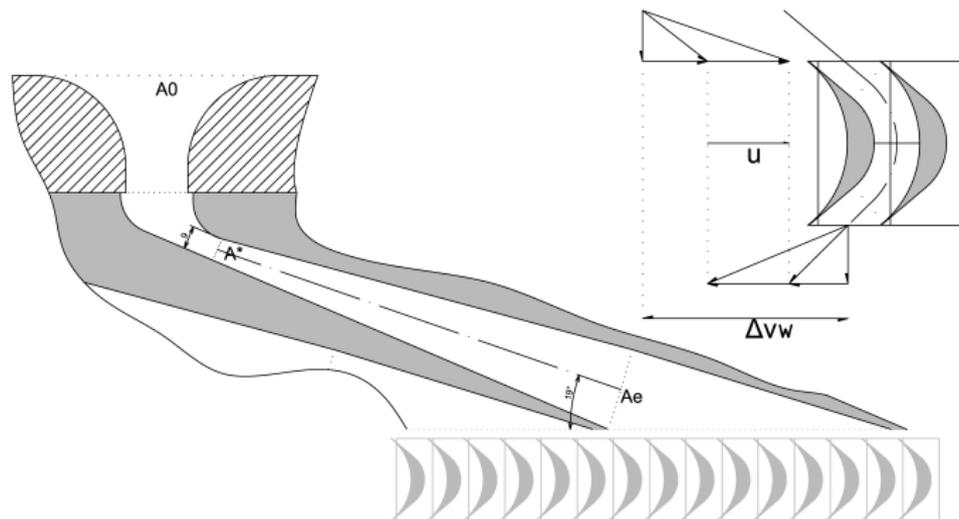


Figure : wrapped section of turbine nozzle and rotor

## Turbine IV

Based on Stodola's Law of Cones [4] [5], Cooke [2] [1] proposed a model for multi-stage steam turbines:

$$\dot{m}_{turb} = k_T \times \sqrt{\rho_{in} \times p_{in}} \times \sqrt{1 - \left(\frac{p_{out}}{p_{in}}\right)^{\frac{\kappa+1}{\kappa}}} \quad (1)$$

The exponents of the pressure ratio  $r_s$  is usually set to 2 for steam turbines. The question is: what happens if one uses the  $\kappa$  of the organic fluid?

→ two model variants are tested:  $\kappa = constant$ ,  $\kappa = f(p, T)$

# Turbine V

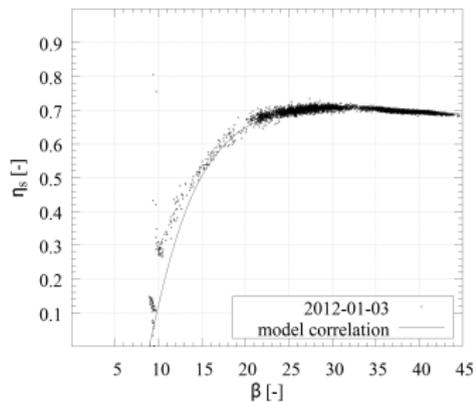


Figure : measured isentropic efficiency of turbine vs. correlation

$$\eta_s = a \times \operatorname{atan} \left( b \times \beta^2 + \frac{c}{\beta} \right) + d \times \beta + f \quad (2)$$

# Alternator I

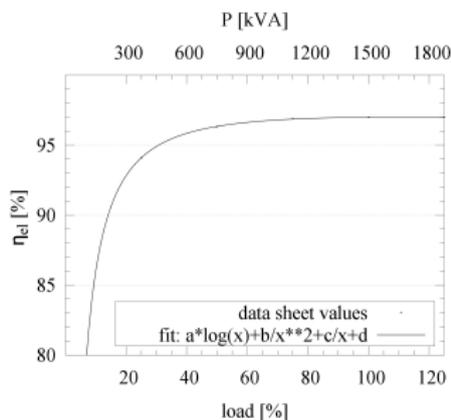


Figure : electric efficiency of alternator

- synchronous engine ( $50 \pm 0.5$  Hz), rated power 1500 kVA
- water cooled with separate cooling unit

# Drive train I

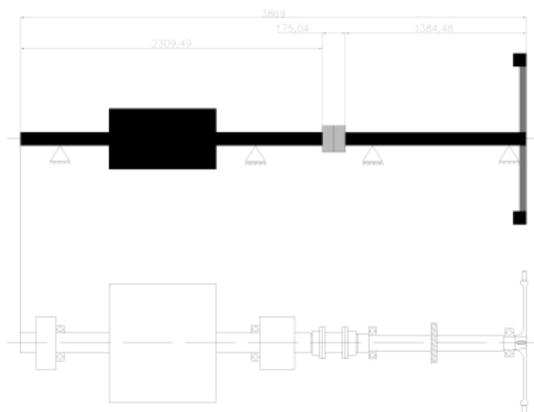


Figure : entire drive train, including bearings and couplings

- the friction has constant, linear and quadratic compounds
- simplification: bearing friction is a quadratic correlation  $f(\omega)$
- tensor is calculated via measured shut down

# Drive train II

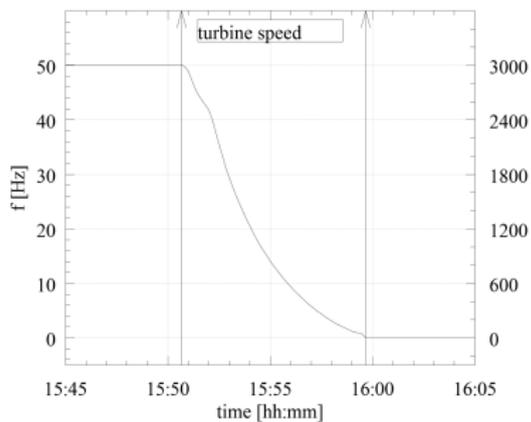


Figure : turbine shut-down vs. time

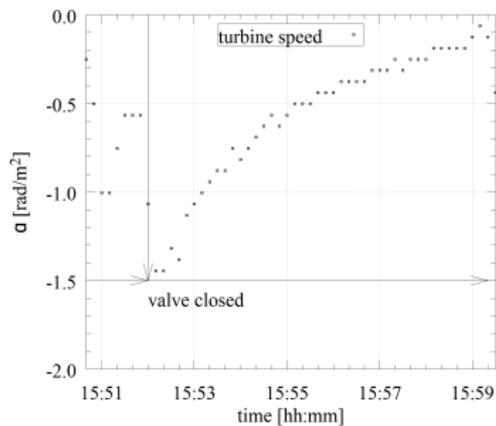


Figure : angular acceleration of rotor

- friction torque max. 63 Nm
- tensor 97.9 kg m<sup>2</sup>

# Results I

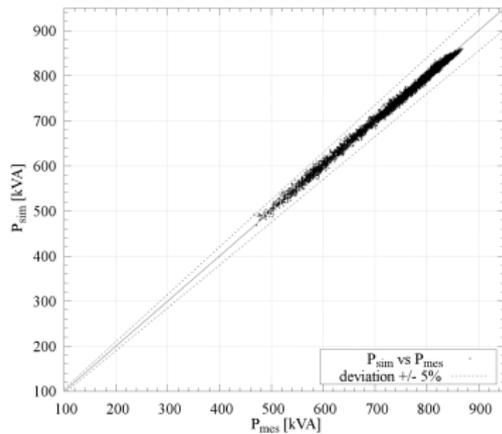


Figure : simulated vs. measured (12-01-01)

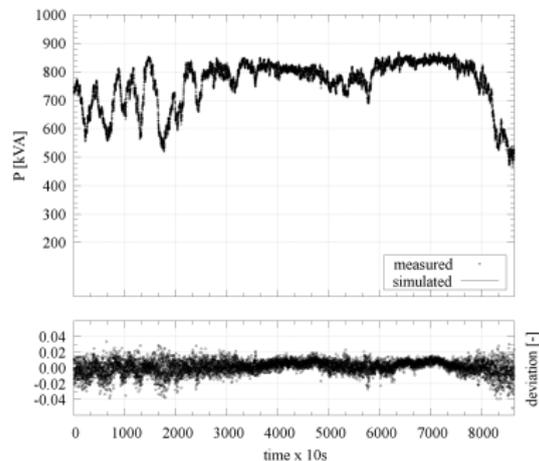


Figure : simulated and deviation vs. time (12-01-01)

# Results II

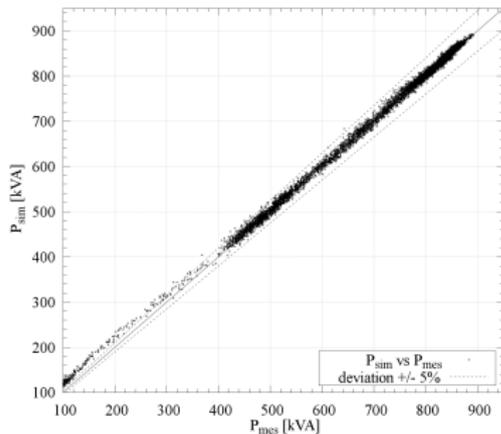


Figure : simulated vs. measured (12-01-02)

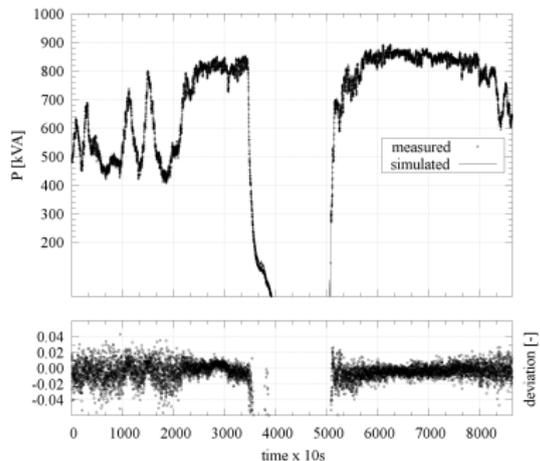


Figure : simulated and deviation vs. time (12-01-02)

## Results III

model	date	measured		simulated		deviation
		$\bar{P}_{el}$	W	$\bar{P}_{el}$	W	
-	[YYMMDD]	[kW]	[kWh]	[kW]	[kWh]	[-]
$\kappa = \bar{\kappa}$	12-01-01	760.28	18247	756.62	18159	-0.4821%
	12-01-02	592.47	14219	589.21	14141	-0.5491%
	12-01-03	338.38	8121	337.09	8090	-0.3823%
$\kappa(p, T)$	12-01-01	760.28	18247	756.62	18159	-0.4824%
	12-01-02	592.47	14219	589.17	18158	-0.5567%
	12-01-03	338.38	8121	337.06	8094	-0.3900%

Table : comparison of model and measured values for three data sets (1 day / 10 second steps)

## Results IV

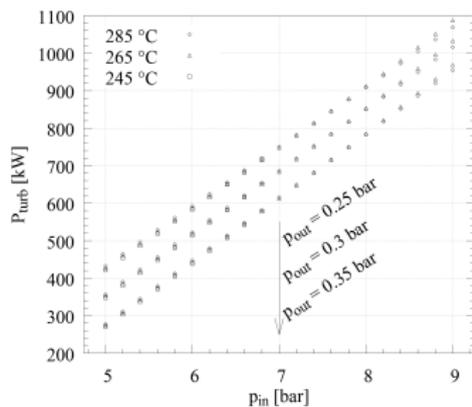


Figure : parameter study of turbine model

→ turbine provides maximum with low super-heating

# Conclusions I

## Conclusions

- measured values of isentropic efficiency give a good prediction for higher pressure ratios ( $\beta \geq 15$ )
- both model variants have a good prediction quality, the  $\kappa = const$ -model needs less CPU
- $k_t$ ,  $\tau_{fric}(\omega)$ , polytropic exp, alternator: 4 parameters,  $\eta_s$  5 parameters
- low super-heating is favourable, possible optimisation of the evaporator level
- for load changes under 10% both models have less than  $\pm 2\%$  dispersion, maximum of  $\pm 5\%$
- for 400 to 900 kW<sub>el</sub> models have less than  $\pm 2\%$  dispersion
- the cumulated work error for one day of operation is less than -0.5%

# Conclusions II

## Next steps

- testing the models with oscillating rotation frequency with data of higher precision

**Thank you for your attention - Bedankt voor uw aandacht!**

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Thanks to the modelica people

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